

微分90題      ※次の関数を微分せよ。

( )組( )番 名前( )

$$(1) \quad y = \frac{x^3 - 2x + 3}{x + 1}$$

$$(2) \quad y = \frac{x - 3}{(x - 1)(x - 2)}$$

$$(3) \quad y = \frac{x^2 - x + 1}{x^2 + x + 1}$$

$$(4) \quad y = \left( \frac{x}{x^2 + 1} \right)^3$$

$$(5) \quad y = \left( \frac{2x + 3}{x^2 - 1} \right)^3$$

$$(6) \quad y = \frac{(x^2 + 1)^2}{(x - 2)^3}$$

$$(7) \quad y = 2x^2 + \sqrt{x - 4}$$

$$(8) \quad y = (2x^2 + 1)\sqrt{2 - x^2}$$

$$(9) \quad y = \frac{x}{\sqrt{x + 1}}$$

$$(10) \quad y = \sqrt{\frac{1 - x}{1 + x}}$$

$$(11) \quad y = x^2 \sqrt{1 - x^2}$$

$$(12) \quad y = \frac{1 - x^2}{\sqrt{1 + x^2}}$$

$$(13) \quad y = (x + \sqrt{x^2 + 1})^2$$

$$(14) \quad y = \frac{1}{x + \sqrt{x^2 - 1}}$$

$$(15) \quad y = \frac{1 - x + 3x^2}{\sqrt{x}}$$

$$(16) \quad y = \left( x - \frac{1}{\sqrt{x}} \right)^2$$

$$(17) \quad y = \frac{x}{\sqrt{4 - x^2}}$$

$$(18) \quad y = \sqrt{\frac{x^2 - 1}{x^2 + 1}}$$

$$(19) \quad y = \sqrt{1 + \sqrt{1 + x}}$$

$$(20) \quad y = \frac{x + \sqrt{x^2 - 1}}{x - \sqrt{x^2 - 1}}$$

$$(21) \quad y = \frac{\sqrt{1 + x^2} - \sqrt{1 - x^2}}{\sqrt{1 + x^2} + \sqrt{1 - x^2}}$$

$$(22) \quad y = (x + 3) \sqrt[3]{3 - 2x}$$

$$(23) \quad y = \sqrt[3]{\frac{(x + 1)^2}{x^2 + 1}}$$

$$(24) \quad y = \sin 2x$$

$$(25) \quad y = \sin x \cos^2 x$$

$$(26) \quad y = \sin^2 x \cos 2x$$

$$(27) \quad y = \sin^2 \frac{x}{2}$$

$$(28) \quad y = \sin^3(3x - \pi)$$

$$(29) \quad y = \frac{1}{\sin^2 x}$$

$$(30) \quad y = \tan^3 \left( 2x - \frac{\pi}{4} \right)$$

$$(31) \quad y = \frac{1 - \sin x}{1 + \sin x}$$

$$(32) \quad y = \frac{1 + \sin x}{\cos^2 x}$$

$$(33) \quad y = \frac{\sin x + \cos x}{\sin x - \cos x}$$

$$(34) \quad y = \sin \sqrt{x^2 + x + 1}$$

$$(35) \quad y = \sqrt{1 - \sin 2x}$$

$$(36) \quad y = \frac{1}{\sqrt{\tan x}}$$

$$(37) \quad y = \sqrt{\frac{1 + \sin x}{1 - \sin x}}$$

$$(38) \quad y = \sqrt{1 + \sin x} + \sqrt{1 - \sin x}$$

$$(39) \quad y = \frac{1}{\sqrt{\sin x + \cos x}}$$

$$(40) \quad y = \sin 2x \tan x$$

$$(41) \quad y = \sin 3x + \cos x^3$$

$$(42) \quad y = \sqrt{3\sin^2 x + 2\cos^2 x}$$

$$(43) \quad y = \frac{\sin x}{\sqrt{4\cos^2 x + 3\sin^2 x}}$$

$$(44) \quad y = e^{-x^3}$$

$$(45) \quad y = a^{x^2+1}$$

(46)  $y = (e^x + e^{-x})^2$

(47)  $y = x e^{-x^2}$

(48)  $y = e^{ax} \cos bx$

(49)  $y = e^{x^2} \sin x$

(50)  $y = \log(x^2 + 1)$

(51)  $y = x \log x$

(52)  $y = \frac{\log x}{x}$

(53)  $y = x^2 (\log x)^3$

(54)  $y = \log_x a$

(55)  $y = \frac{\sqrt{x}}{e^x}$

(56)  $y = \log \frac{e^x + 1}{e^x}$

(57)  $y = a^x \log x$

(58)  $y = x e^{\frac{1}{x}}$

(59)  $y = 2^x \sin x$

(60)  $y = e^{-ax} \sin bx$

(61)  $y = e^{x \sin x}$

(62)  $y = \frac{e^x \cos x}{1 + \sin x}$

(63)  $y = \log \left( \tan x + \frac{1}{\cos x} \right)$

(64)  $y = \log \frac{1 + \sin x}{1 - \sin x}$

(65)  $y = \log |2x - \sqrt{1 + 4x^2}|$

(66)  $y = \log \left| \frac{x-a}{x+a} \right|$

(67)  $y = \log \left| \tan \frac{x}{2} \right|$

(68)  $y = \log \frac{2\sin x + \cos x}{\sin x + 2\cos x}$

(69)  $y = \log \sqrt{\frac{2+x}{2-x}}$

(70)  $y = (x+2)^2 (x+3)^3 (x+4)^4$

(71)  $y = \frac{(x+1)^3}{(x+2)^2 (x+3)^4}$

(72)  $y = \sqrt{\frac{(x-1)(x+3)}{(x+1)^3}}$

(73)  $y = \sqrt{\frac{(x-1)^3}{(x^2+1)(x+1)}}$

(74)  $y = \sin(\log x)$

(75)  $y = \tan(\sin x)$

(76)  $y = \log(\log x)$

(77)  $y = \log(\sin^2 x)$

(78)  $y = \log \{e^x (1-x)\}$

(79)  $y = \frac{1}{2} \{(\log x)^2 + 1\}$

(80)  $y = x^x \quad (x > 0)$

(81)  $y = x^{\log x} \quad (x > 0)$

(82)  $y = x^{\sin x} \quad (x > 0)$

(83)  $y = (\tan x)^{\sin x} \quad (0 < x < \frac{\pi}{2})$

(84)  $y = (\sin x)^{\sqrt{\log x}} \quad (x > 0)$

(85)  $y = \log(\log(\log x))$

(86)  $y = \sin(\sin(\sin x)) \quad (0 < x < \frac{\pi}{2})$

(87)  $y = x^2 \sqrt{\frac{1+x^2}{1-x^2}}$

(88)  $y = \sqrt{\frac{1-\sqrt[3]{x}}{1+\sqrt[3]{x}}}$

(89)  $x = y\sqrt{1+y}$

(90)  $2x^2 + 4xy + 5y^2 = 1$